

Answers to selected questions

PL- Day 1

3. If two coplanar lines are cut by a transversal so that the alternate interior angles formed are congruent, then the two lines are parallel.
4. If two coplanar lines are cut by a transversal so that the corresponding angles are congruent, then the two lines are parallel.
5. If two coplanar lines are cut by a transversal so that the interior angles on the same side of the transversal are supplementary, then the lines are parallel.
6. Vertical angles ($\angle 2$ and $\angle 4$) are congruent. If two coplanar lines are cut by a transversal so that the interior angles on the same side of the transversal are supplementary, then the lines are parallel.
7. Vertical angles ($\angle 2$ and $\angle 4$) are congruent. If two coplanar lines are cut by a transversal so that the corresponding angles are congruent, then the lines are parallel.

8. Vertical angles ($\angle 7$ and $\angle 5$) are congruent. If two coplanar lines are cut by a transversal so that the interior angles on the same side of the transversal are supplementary, then the lines are parallel.

11. $m\angle A + m\angle B = 3x + (180 - 3x) = 180$. Since interior angles on the same side of the transversal \overline{AB} are supplementary, $\overline{AD} \parallel \overline{BC}$.

PL – Day 2

3. 80 4. 150 5. 120
6. 75 7. 115 8. 50
9. 42 10. 80 11. 65
12. 60 13. 44 and 136 14. 21 and 21
15. a. $m\angle 1 = 70, m\angle 2 = 110, m\angle 3 = 70, m\angle 4 = 50,$
 $m\angle 5 = 130, m\angle 6 = 50, m\angle 7 = 50, m\angle 8 = 60,$
 $m\angle 9 = 70$
b. 120 c. Yes d. 120
e. 110 f. 130 g. 180
16. $m\angle A = m\angle C = 75; m\angle ABC = m\angle D = 105$

PL - Day 3

3. Perpendicular 4. Parallel 5. Parallel
6. Neither parallel nor perpendicular
7. Parallel 8. Perpendicular
9. $y = -3x + 4$ 10. $y = \frac{1}{3}x + 4$
11. $y = \frac{1}{2}x + 3$ 12. $y = -3$

Applying Skills

13. a. $-\frac{1}{2}$ b. $-\frac{1}{2}$ c. $y = -\frac{1}{2}x + 6$
d. 3 e. 3 f. $y = 3x - 1$
g. (2, 5)

PL – Day 4

3. Yes 4. No 5. No
6. Yes 7. 40 8. 50
9. 54 10. 50 11. 80
12. 45 13. 52 14. 35
15. 20 16. 140 17. 90
18. 54 19. 120
20. $m\angle ACD = 60; m\angle ACB = 120$
21. $m\angle ACD = 90; m\angle ACB = 90$
22. $m\angle ACD = 60; m\angle B = 20$
23. $m\angle B = 95; m\angle ACD = 135; m\angle ACB = 45$

Applying Skills

24. $46^\circ, 67^\circ, 67^\circ$ 25. $70^\circ, 55^\circ, 55^\circ$ 26. $20^\circ, 80^\circ, 80^\circ$
27. $m\angle N = 58$; measure of exterior angle = 122
28. a. $m\angle A = 72; m\angle B = 67; m\angle C = 41$ b. \overline{BC}
29. $m\angle A = m\angle C = 30; m\angle B = 120$; measure of exterior angle = 60

PL – Day 5

3. Yes, by AAS. 4. Yes, by AAS.
5. No. AAA is insufficient to prove congruence.
6. Yes, by AAS.
7. No. SSA is insufficient to prove congruence.
8. Yes, by SAS.

Applying Skills

9. Let $\triangle ABC \cong \triangle DEF$, so $\angle A \cong \angle D$ and $\overline{AC} \cong \overline{DF}$. Draw \overline{CG} , the altitude from $\angle A$ in $\triangle ABC$, and \overline{FH} , the altitude from $\angle F$ in $\triangle DEF$, to form right triangles $\triangle ABG$ and $\triangle DFH$. Two right triangles are congruent if the hypotenuse and an acute angle of one right triangle are congruent to the hypotenuse and an acute angle of the other right triangle, so $\triangle ACG \cong \triangle DFH$. Corresponding parts of congruent triangles are congruent, so the altitudes, \overline{CG} and \overline{FH} , are congruent. ■

PL – Day 6

7. $x = 4$ 8. $PR = RQ = 21$
 9. $m\angle R = 72; m\angle N = 36$
 10. $AB = AC = 36; BC = 46$

PL – Day 7

Proofs

PL – Day 8

3. a. 180 b. 900 c. 1,260
 4. a. 360 b. 1,080 c. 540 d. 1,440
 5. a. 360 b. 360 c. 360 d. 360
 6. a. 90 b. 90
 7. a. 72 b. 108
 8. a. 60 b. 120
 9. a. 45 b. 135
 10. a. 40 b. 140
 11. a. 30 b. 150
 12. a. 18 b. 162
 13. a. 10 b. 170
 14. a. $8\frac{4}{7}$ b. $171\frac{3}{7}$
 15. a. 12 b. 8 c. 6 d. 3
 16. a. 4 b. 6 c. 9 d. 18
 17. a. 3 b. 4 c. 5 d. 7
 e. 10 f. 17 g. 12 h. 22

PL – Day 9 Review

1. 15 2. 30 3. 24 4. 55
 5. a. 18 b. 72 c. 72 d. 108 e. 72

6. 30 7. 6 8. 36
 9. 42, 48, 90 10. 120 11. 80
 12. 40 13. 154 14. 60
 15. 28 16. 20, 80, 80 17. 90
 18. 30 19. 12 20. 1,260

21. In $\triangle ABC$, $\angle C$ is a right angle so $m\angle C = 90$.
 Therefore, $m\angle B < 90$ since $\angle B$ are complementary so $\angle B$ must be acute. If the measures of two angles of a triangle are unequal, the lengths of the sides opposite these angles are unequal and the longer side lies opposite the larger angle. Therefore, $AB > AC$. ■
22. Since \overline{AE} and \overline{CE} bisect each other, $\overline{AE} \cong \overline{EB}$ and $\overline{CE} \cong \overline{ED}$. Vertical angles are congruent, so $\angle AEC \cong \angle BED$. Therefore, $\angle AEC \cong \angle BED$ by SAS. Corresponding parts of congruent triangles are congruent, so $\angle EAC \cong \angle EBD$. If two coplanar lines are cut by a transversal so that the alternate interior angles formed are congruent, then the two lines are parallel. Therefore, $\overline{AC} \parallel \overline{BD}$. ■

23. In $\triangle BPA$, $\overline{BP} \cong \overline{CP}$, so by the isosceles triangle theorem $\angle PBC \cong \angle PCB$. $\angle PBA$ and $\angle PBC$ form a linear pair, so they are supplementary. Also, $\angle PCD$ and $\angle PCB$ form a linear pair, so they are supplementary. If two angles are congruent, then their supplements are congruent, so $\angle PBA \cong \angle PCD$. It is given that $\angle APB \cong \angle DPC$, so $\triangle ABP \cong \triangle DCP$ by ASA. Corresponding parts of congruent triangles are congruent, so $\overline{PA} \cong \overline{PD}$. ■
24. In $\triangle BPC$, $\angle PBC \cong \angle PCB$. If two angles of a triangle are congruent, then the sides opposite these angles are congruent, so $\overline{PB} \cong \overline{PC}$. It is given that $\angle PBC \cong \angle PCB$. $\angle PBA$ and $\angle PBC$ form a linear pair, so they are supplementary. Also, $\angle PCD$ and $\angle PCB$ form a linear pair, so they are supplementary. If two angles are congruent, then their supplements are congruent, so $\angle PBA \cong \angle PCD$. Since $\overline{AB} \cong \overline{DC}$, $\triangle ABP \cong \triangle DCP$ by SAS. Corresponding parts of congruent triangles are congruent, so $\overline{PA} \cong \overline{PD}$. ■
25. No. The sum of the measures of the interior angles of a pentagon is 540 degrees, and angles A , B , C , and D have measures which already sum to 540. Since $m\angle E \neq 0$, Herbie's pentagon is not possible.